## Mapping electron transport pathways in complex systems

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## Local properties are central in our understanding of chemistry



		-			
	SUBSTITUENT CONSTANTS				
Bahat.	Constant	Bearce	No. of reactions	Prohabile	++0-
ANH:	-0.000	2	2	Sec.	
PCH O	- 268	1	21	0.077	3/
pC <sub>1</sub> H <sub>1</sub> O	25	3	6	.105	8
3,4-di CH.	239		1	- 4.4	1
w(CH_)N	211	31	1		7
p(CH <sub>2</sub> ) <sub>2</sub> N	- 205	21*	- 2 -		170
PCH <sub>4</sub>	170	1	33	.046	+34/ / u
mNH:	101	2	3	.060	1 1
3.4CH <sub>i</sub> O <sub>i</sub>	159	2	3	.023	
pC.H.	144	2	1		5 61
mCH,	- 069	1	21	.038	9 1
pCH <sub>5</sub>	047	2	1		3 / / /
None	.000	I	36	.034	+2.0 - 6 7
pC.H.	+ 009	2	8	22	11
pē	+ .062	1	7	.066	174
mCH <sub>i</sub> O	+ 115	1	7	.116	1 2 6
mCiHiO	+ .15	3	2	1.4.4	
#C.R.*	+ 17	3	.9.	.102	1 18
¢C1	+ 227	1	31	.040	+1.0 -
pBr	+ .232	1	24	040	1 /2
14	+ .276	2	11	073	9
1012	+ .337	1	5	083	
-17	+ 352	I	8	.039	
mCi	+ .373	1	19	100.	
mBr	+ .391		17	.035	
C.H.N.	+ 640	26, 27	1	1.1.4	-95 0
MCN	+ .878	26,27	1		
MNO,	+ 710	1	21	069	Fig. 1-Relationship he
pNO <sub>i</sub> (b)	+ 778	1	18	060	and a for various reactions
PCN	+1.000			042	III). The position of the
pNO <sub>2</sub> (a) <sup>d</sup>	+1.27	3	8	0.52	dinates is arbitrary.
A REAL PROPERTY.					

L. P. Hammett JACS (1937) 59, 96

- From Hammett constants, to Mulliken charges to local spins, local properties underpin structure-function relationships in chemistry.
- For new types of physical measurements, like passing current through a molecule, we need new local descriptions.
- If we can understand how different components interact in a complex system, maybe we can design interesting devices?



## Questions:



- How do different functional groups in a molecule modulate transport? Do they always participate?
- Does current through a molecule always follow the bonds?
- When might through-space interactions be important? Is overlap all that matters?
- Can we map the characteristic transport pathways through a complex molecular system?

## Calculating conductance



 $T = \operatorname{Tr}[\Gamma_L G^r \Gamma_R G^a]$ 

#### Calculating current from transmission



$$I(V) = \frac{2e}{h} \int_{-\infty}^{\infty} dE \operatorname{Tr}[\Gamma_L G^r \Gamma_R G^a](f_L - f_R)$$



## Current through an arbitrary surface



 $I_{mn} = \frac{2e}{\hbar} \int \frac{d\varepsilon}{2\pi} K_{mn}(\varepsilon) \qquad I = \frac{2e}{\hbar} \sum_{m \in M_L} \sum_{n \in M_R} \int d\varepsilon K_{mn}(\varepsilon)$ 

 $\sum K_{mn}(\mathbf{\varepsilon}) = (f_L(\mathbf{\varepsilon}) - f_R(\mathbf{\varepsilon}))T(\mathbf{\varepsilon})$  $m \in M_L n \in M_R$ 

 $K_{mn}(\varepsilon) = \sum_{i \in m} \sum_{\substack{j \in n \\ n \neq m}} \sum_{kl} (if_L(V_{ij}G_{jk}^r\Gamma_{kl}^LG_{li}^a - V_{ji}G_{il}^r\Gamma_{lk}^LG_{kj}^a)$  $-if_R(V_{ji}G_{il}^r\Gamma_{lk}^RG_{kj}^a - V_{ij}G_{jk}^r\Gamma_{kl}^RG_{lj}^a))$ 

Nature Chem. 2, 223-228 (2010)

## Conservation



## What does local transmission look like?



A note about local transmission plots:

- The radius of the arrow is proportional to the magnitude of the local transmission
- The arrows are normalized so the largest component in each picture is the same size.
- The arrows are only shown for elements that are greater than 10% of the maximum local transmission element.
- The arrows are sometimes coloured red and blue to indicate transmission in the forward and reverse direction.

Nature Chem. 2, 223-228 (2010)

## More involved local transmission



Nature Chem. 2, 223-228 (2010)

#### **π** transmission & Total transmission



#### **Cross-conjugated molecules**



"a compound possessing three unsaturated groups, two of which although conjugated to a third unsaturated center are not conjugated to each other." N. F. Phelan, M. Orchin, J. Chem. Educ. **45**, 633 (1968)

## Similar behavior



#### $\sigma$ -systems can be unusual too





## We can see the signature of interference



Nature Chem. 2, 223-228 (2010)

## Designing molecular electronic devices.... ....means assembling molecules

- Positioning single molecules between metallic electrodes is an enormous challenge.
- Controllable synthesis of really large molecules is another enormous challenge.
- Self-assembly of supramolecular structures or carefully constructed films seem to be a promising alternative.

![](_page_14_Figure_4.jpeg)

J. Heath and M. Ratner, Physics Today, May 2003

![](_page_14_Figure_6.jpeg)

J. Heath

![](_page_14_Picture_8.jpeg)

M. Reed and J. Tour Scientific American, June 2000

## π-stacked structures are favorable for self-assembly

0

![](_page_15_Picture_1.jpeg)

J.A.A.W. Elemans, A. E. Rowan and R. J. M. Nolte J. Mater. Chem. (2003) **13** 2661

- Non-bonding interactions can be used to build extremely large structures.
- These structures have been suggested as architectures for charge transport.
  - What is really desirable for charge transport in a  $\pi$ -stacked system?

![](_page_15_Figure_6.jpeg)

![](_page_15_Picture_7.jpeg)

R. van Hameren et al. Science (2006) **314** 1433

## Take a simple series

![](_page_16_Figure_1.jpeg)

## Increasing transmission by reducing overlap

![](_page_17_Figure_1.jpeg)

#### Perturbing interference features

![](_page_18_Figure_1.jpeg)

## Putting it all together: the super stacker

conducting AFM

Au surface

short aliphatic chain forces alignment between aromatic units

Alkene-thiols connect the stacker to the Au contacts

Hydrogen bonds

stabilize the  $\pi$ -stacker

J. Am. Chem. Soc. 133, 2242-2249 (2011)

HO

HO.

OH

OH

## Pulling the super stacker

Nonequilibrium trajectory

Pulling speed ~ 10<sup>-3</sup> Å/ps

k = I.I N/m

J. Am. Chem. Soc. 133, 2242-2249 (2011)

#### Mechanically activated molecular switch

![](_page_21_Figure_1.jpeg)

#### Agreement between transport methods

![](_page_22_Figure_1.jpeg)

Methods agree in average, disagree for individual conformations

# Bistability leads to blinking in the conductance

![](_page_23_Figure_1.jpeg)

## The cow diagram: understanding transport domains

![](_page_24_Figure_1.jpeg)

J. Am. Chem. Soc. 133, 2242-2249 (2011)

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![](_page_25_Picture_5.jpeg)

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